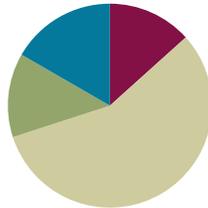


## Lesson 15

**Objective:** Add measurements using the standard algorithm to compose larger units once.

### Suggested Lesson Structure

■ Fluency Practice	(8 minutes)
■ Application Problem	(8 minutes)
■ Concept Development	(34 minutes)
■ Student Debrief	(10 minutes)
<b>Total Time</b>	<b>(60 minutes)</b>



### Fluency Practice (8 minutes)

- Part–Whole with Measurement Units **3.MD.2** (3 minutes)
- Round Three- and Four-Digit Numbers **3.NBT.1** (5 minutes)

### Part–Whole with Measurement Units (3 minutes)

Materials: (S) Personal white board

Note: This activity reviews part–whole thinking using measurement units.

T: There are 100 centimeters in 1 meter. How many centimeters are in 2 meters?

S: 200 centimeters.

T: 3 meters?

S: 300 centimeters.

T: 8 meters?

S: 800 centimeters.

T: (Write  $50 \text{ minutes} + \underline{\quad} \text{ minutes} = 1 \text{ hour}$ .) There are 60 minutes in 1 hour. On your personal white board, fill in the equation.

S: (Write  $50 \text{ minutes} + 10 \text{ minutes} = 1 \text{ hour}$ .)

Continue with the following suggested sequence: 30 minutes and 45 minutes.

T: (Write  $800 \text{ mL} + \underline{\quad} \text{ mL} = 1 \text{ L}$ .) There are 1,000 milliliters in 1 liter. On your board, fill in the equation.

S: (Write  $800 \text{ mL} + 200 \text{ mL} = 1 \text{ L}$ .)

Continue with the following suggested sequence: 500 mL, 700 mL, and 250 mL.

T: (Write  $1 \text{ kg} - 500 \text{ g} = \underline{\hspace{1cm}}$  g.) There are 1,000 grams in 1 kilogram. On your board, fill in the equation.

S: (Write  $1 \text{ kg} - 500 \text{ g} = 500 \text{ g}$ .)

Continue with the following suggested sequence: Subtract 300 g, 700 g, and 650 g from 1 kg.

### Round Three- and Four-Digit Numbers (5 minutes)

Materials: (S) Personal white board

Note: This activity reviews rounding from Lessons 13 and 14.

T: (Write  $87 \approx \underline{\hspace{1cm}}$ .) What is 87 rounded to the nearest ten?

S: 90.

Continue with the following possible sequence: 387, 43, 643, 35, and 865.

T: (Write  $237 \approx \underline{\hspace{1cm}}$ .) 237 is between which 2 hundreds?

S: 200 and 300.

T: On your board, draw a vertical number line. Mark 200 and 300 as your endpoints and label the halfway point.

S: (Label 200 and 300 as endpoints and 250 as the halfway point.)

T: Show where 237 falls on the number line, and then round to the nearest hundred.

S: (Plot 237 between 200 and 250 and write  $237 \approx 200$ .)

Continue with the following suggested sequence: 1,237; 678; 1,678; 850; 1,850; and 2,361.

### Application Problem (8 minutes)

Use mental math to solve these problems. Record your strategy for solving each problem.

a.  $46 \text{ mL} + 5 \text{ mL}$

b.  $39 \text{ cm} + 8 \text{ cm}$

c.  $125 \text{ g} + 7 \text{ g}$

d.  $108 \text{ L} + 4 \text{ L}$

Possible strategies:

a.  $46 \text{ mL} + 4 \text{ mL} + 1 \text{ mL} = 50 \text{ mL} + 1 \text{ mL} = 51 \text{ mL}$

b.  $39 \text{ cm} + 1 \text{ cm} + 7 \text{ cm} = 40 \text{ cm} + 7 \text{ cm} = 47 \text{ cm}$

c.  $125 \text{ g} + 5 \text{ g} + 2 \text{ g} = 130 \text{ g} + 2 \text{ g} = 132 \text{ g}$

d.  $108 \text{ L} + 2 \text{ L} + 2 \text{ L} = 110 \text{ L} + 2 \text{ L} = 112 \text{ L}$

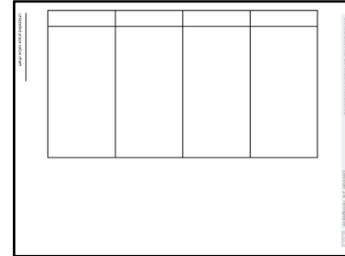
Note: This problem is designed to show that mental math can be an efficient strategy even when renaming is required. It also sets up the conversation in the Student Debrief about when and why the standard algorithm is used. Be sure to give students an opportunity to discuss and show how they solved these problems.

**Concept Development (34 minutes)**

Materials: (T) 2 beakers, water (S) Unlabeled place value chart (Lesson 14 Template), place value disks, personal white board

Students start with the unlabeled place value chart template in their personal white boards.

Lesson 14 Template



T: (Show Beaker A with 56 milliliters of water and Beaker B with 27 milliliters of water.) Beaker A has 56 milliliters of water, and Beaker B has 27 milliliters of water. Let’s use place value charts and place value disks to find the total milliliters of water in both beakers.

T: Use place value disks to represent the amount of water from Beaker A on your chart. (Allow time for students to work.)

T: Record 56 milliliters in the workspace on your personal white board below the place value chart.

T: Leave the disks for 56 on your chart. Use more disks to represent the amount of water from Beaker B. Place them below your model of 56. (Allow time for students to work.)

T: In the workspace on your board, use an addition sign to show that you added 27 milliliters to 56 milliliters.

T: (Point to the place value disks in the ones column.) Six ones plus 7 ones equals ...?

S: 13 ones.

T: We can change 10 ones for 1 ten. Take 10 ones disks and change them for 1 tens disk. Where do we put the tens disk on the place value chart?

S: In the tens column.

T: How many ones do we have now?

S: 3 ones!

T: Let’s show that same work in the problem we wrote in our workspace on our boards. If you wrote your problem horizontally, rewrite it vertically so that it looks like mine.

$$\begin{array}{r} 56 \text{ mL} \\ + 27 \text{ mL} \\ \hline \end{array}$$

T: (Point to the ones.) 6 ones plus 7 ones equals ...?

S: 13 ones.

T: Let’s rename some ones as tens. How many tens and ones in 13 ones?

S: 1 ten and 3 ones.



**NOTES ON MULTIPLE MEANS OF ACTION AND EXPRESSION:**

English language learners and others will benefit from the real-world context, the varied methods for response (personal white boards, models, numbers, etc.), and the introduction to academic math language (*standard algorithm*) at the end of the lesson.

T: This is how we show renaming using the **standard algorithm**. (Write the 1 so that it crosses the line under the tens in the tens place and the 3 below the line in the ones column. This way you write 13 rather than 3 and 1 as separate numbers. Refer to the vertical addition shown to the right.) Show this work on your board.

$$\begin{array}{r} 56 \text{ mL} \\ + 27 \text{ mL} \\ \hline 13 \\ \hline 83 \end{array}$$

- T: Talk to a partner. How is this work similar to the work we did with the place value disks?  
 S: (Discuss.)  
 T: That’s right. Renaming in the algorithm is the same as changing with our place value disks.  
 T: (Point to the place value disks in the tens column.) 5 tens plus 2 tens plus 1 ten equals...?  
 S: 8 tens!  
 T: 8 tens 3 ones makes how many milliliters of water in the bowl?  
 S: 83 milliliters.  
 T: Let’s show that in our problem. (Point to the tens.) 5 tens plus 2 tens plus 1 ten equals...?  
 S: 8 tens.  
 T: Record 8 tens below the line in the tens column.  
 T: What unit do we need to include in our answer?  
 S: Milliliters!  
 T: Read the problem with me. (Point and read.) 56 milliliters plus 27 milliliters equals 83 milliliters. We just used the standard algorithm as a tool for solving this problem.  
 T: How can I check our work using the beaker?  
 S: Pour the water from one beaker into the other beaker and read the measurement.  
 T: (Pour.) The amount of water in the beaker is 83 milliliters!

$$\begin{array}{r} 56 \text{ mL} \\ + 27 \text{ mL} \\ \hline 83 \text{ mL} \end{array}$$

Continue with the following suggested problems:

- *Add to with start unknown*: Lisa draws a line on the board. Marcus shortens the length of the line by erasing 32 centimeters. The total length of the line is now 187 centimeters. How long is the line that Lisa drew?
- *Compare with bigger unknown (start unknown)*: John reads for 74 minutes on Wednesday. On Thursday, he reads for 17 more minutes than he read on Wednesday. How many total minutes does John read on Wednesday and Thursday?

**Problem Set (10 minutes)**

Students should do their personal best to complete the Problem Set within the allotted 10 minutes. For some classes, it may be appropriate to modify the assignment by specifying which problems they work on first. Some problems do not specify a method for solving. Students should solve these problems using the RDW approach used for Application Problems.

 **NOTES ON THE PROBLEM SET:**

The problems in the Problem Set are written horizontally so that students do not assume that they need to use the standard algorithm to solve. Mental math may be a more efficient strategy in some cases. Invite students to use the algorithm as a strategic tool, purposefully choosing it rather than defaulting to it.

**Student Debrief (10 minutes)**

**Lesson Objective:** Add measurements using the standard algorithm to compose larger units once.

The Student Debrief is intended to invite reflection and active processing of the total lesson experience.

Invite students to review their solutions for the Problem Set. They should check work by comparing answers with a partner before going over answers as a class. Look for misconceptions or misunderstandings that can be addressed in the Debrief. Guide students in a conversation to debrief the Problem Set and process the lesson.

Any combination of the questions below may be used to lead the discussion.

**MP.7**

- Notice the units in Problems 1(j) and 1(k). Both problems use both kilograms and grams. Did having two units in the problem change anything about the way you solved?
- What pattern did you notice between Problems 1(a), 1(b), and 1(c)? How did this pattern help you solve the problems?
- Did you rewrite any of the horizontal problems vertically? Why?
- Which problems did you solve using mental math? The **standard algorithm**? Why did you use the standard algorithm for some problems and mental math for other problems? Think about the strategies you used to solve today's Application Problem to help you answer this question.
- Explain to your partner how you used the standard algorithm to solve Problem 3. Did you rename the ones? Tens? Hundreds?
- Explain to your partner what your tape diagram looked like for Problem 4.
- How are Problems 2 and 4 similar? How are they different from the other problems?

NYS COMMON CORE MATHEMATICS CURRICULUM Lesson 15 Problem Set 3•2

Name: Gina Date: \_\_\_\_\_

1. Find the sums below. Choose mental math or the algorithm.

a.  $46 \text{ mL} + 5 \text{ mL}$   
 $\begin{array}{r} 46 \\ + 5 \\ \hline 51 \end{array}$   
 51 mL

b.  $46 \text{ mL} + 25 \text{ mL}$   
 $\begin{array}{r} 46 \\ + 25 \\ \hline 71 \end{array}$   
 71 mL

c.  $46 \text{ mL} + 125 \text{ mL}$   
 $\begin{array}{r} 46 \\ + 125 \\ \hline 171 \end{array}$   
 171 mL

d.  $59 \text{ cm} + 30 \text{ cm}$   
 $\begin{array}{r} 59 \\ + 30 \\ \hline 89 \end{array}$   
 89 cm

e.  $509 \text{ cm} + 83 \text{ cm}$   
 $\begin{array}{r} 509 \\ + 83 \\ \hline 592 \end{array}$   
 592 cm

f.  $597 \text{ cm} + 30 \text{ cm}$   
 $\begin{array}{r} 597 \\ + 30 \\ \hline 627 \end{array}$   
 627 cm

g.  $29 \text{ g} + 63 \text{ g}$   
 $\begin{array}{r} 29 \\ + 63 \\ \hline 92 \end{array}$   
 92 g

h.  $345 \text{ g} + 294 \text{ g}$   
 $\begin{array}{r} 345 \\ + 294 \\ \hline 639 \end{array}$   
 639 g

i.  $480 \text{ g} + 476 \text{ g}$   
 $\begin{array}{r} 480 \\ + 476 \\ \hline 956 \end{array}$   
 956 g

j.  $1 \text{ L } 245 \text{ mL} + 2 \text{ L } 412 \text{ mL}$   
 $\begin{array}{r} 1 \text{ L } 245 \text{ mL} \\ + 2 \text{ L } 412 \text{ mL} \\ \hline 3 \text{ L } 657 \text{ mL} \end{array}$

k.  $2 \text{ kg } 509 \text{ g} + 3 \text{ kg } 367 \text{ g}$   
 $\begin{array}{r} 2 \text{ kg } 509 \text{ g} \\ + 3 \text{ kg } 367 \text{ g} \\ \hline 5 \text{ kg } 876 \text{ g} \end{array}$

COMMON CORE Lesson 15: Add measurements using the standard algorithm to compose larger units once. 6/8/14 Date: \_\_\_\_\_ engage<sup>ny</sup> 2.D.9

NYS COMMON CORE MATHEMATICS CURRICULUM Lesson 15 Problem Set 3•2

2. Nadine and Jen buy a small bag of popcorn and a pretzel at the movie theater. The pretzel weighs 63 grams more than the popcorn. What is the weight of the pretzel?

Pop:  $\boxed{44 \text{ g}}$   $\boxed{63 \text{ g}}$   
 Pretz:  $\boxed{?}$

$\begin{array}{r} 44 \text{ g} \\ + 63 \text{ g} \\ \hline 107 \text{ g} \end{array}$

The pretzel weighs 107 grams.

3. In math class, Jason and Andrea find the total liquid volume of water in their beakers. Jason says the total is 782 milliliters, but Andrea says it is 792 milliliters. The amount of water in each beaker can be found in the table to the right. Show whose calculation is correct. Explain the mistake of the other student.

Student	Liquid Volume
Jason	475 mL
Andrea	317 mL

$\begin{array}{r} 475 \text{ mL} \\ + 317 \text{ mL} \\ \hline 792 \text{ mL} \end{array}$

Andrea is correct. Jason forgot to rename some ones as tens. Or he forgot to add the ten he renamed to the 7 tens and 1 ten that were already there.

4. It takes Greg 15 minutes to mow the front lawn. It takes him 17 more minutes to mow the back lawn than the front lawn. What is the total amount of time Greg spends mowing the lawns?

F:  $\boxed{15 \text{ min}}$   $\boxed{17 \text{ min}}$   
 B:  $\boxed{?}$

$15 \text{ min} + 17 \text{ min} = 32 \text{ min}$

$\begin{array}{r} 32 \text{ min} \\ + 15 \text{ min} \\ \hline 47 \end{array}$

Greg spends 47 minutes mowing lawns.

COMMON CORE Lesson 15: Add measurements using the standard algorithm to compose larger units once. 6/8/14 Date: \_\_\_\_\_ engage<sup>ny</sup> 2.D.10

**Exit Ticket (3 minutes)**

After the Student Debrief, instruct students to complete the Exit Ticket. A review of their work will help with assessing students' understanding of the concepts that were presented in today's lesson and planning more effectively for future lessons. The questions may be read aloud to the students.

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the sums below. Choose mental math or the algorithm.

a.  $46 \text{ mL} + 5 \text{ mL}$

b.  $46 \text{ mL} + 25 \text{ mL}$

c.  $46 \text{ mL} + 125 \text{ mL}$

d.  $59 \text{ cm} + 30 \text{ cm}$

e.  $509 \text{ cm} + 83 \text{ cm}$

f.  $597 \text{ cm} + 30 \text{ cm}$

g.  $29 \text{ g} + 63 \text{ g}$

h.  $345 \text{ g} + 294 \text{ g}$

i.  $480 \text{ g} + 476 \text{ g}$

j.  $1 \text{ L } 245 \text{ mL} + 2 \text{ L } 412 \text{ mL}$

k.  $2 \text{ kg } 509 \text{ g} + 3 \text{ kg } 367 \text{ g}$

2. Nadine and Jen buy a small bag of popcorn and a pretzel at the movie theater. The pretzel weighs 63 grams more than the popcorn. What is the weight of the pretzel?



? grams



44 grams

3. In math class, Jason and Andrea find the total liquid volume of water in their beakers. Jason says the total is 782 milliliters, but Andrea says it is 792 milliliters. The amount of water in each beaker can be found in the table to the right. Show whose calculation is correct. Explain the mistake of the other student.

Student	Liquid Volume
Jason	475 mL
Andrea	317 mL

4. It takes Greg 15 minutes to mow the front lawn. It takes him 17 more minutes to mow the back lawn than the front lawn. What is the total amount of time Greg spends mowing the lawns?

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the sums below. Choose mental math or the algorithm.

a.  $24 \text{ cm} + 36 \text{ cm}$

b.  $562 \text{ m} + 180 \text{ m}$

c.  $345 \text{ km} + 239 \text{ km}$

2. Brianna jogs 15 minutes more on Sunday than Saturday. She jogged 26 minutes on Saturday.

a. How many minutes does she jog on Sunday?

b. How many minutes does she jog in total?

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Find the sums below. Choose mental math or the algorithm.

a.  $75 \text{ cm} + 7 \text{ cm}$

c.  $362 \text{ mL} + 229 \text{ mL}$

e.  $451 \text{ mL} + 339 \text{ mL}$

b.  $39 \text{ kg} + 56 \text{ kg}$

d.  $283 \text{ g} + 92 \text{ g}$

f.  $149 \text{ L} + 331 \text{ L}$

2. The liquid volume of five drinks is shown below.

Drink	Liquid Volume
Apple juice	125 mL
Milk	236 mL
Water	248 mL
Orange juice	174 mL
Fruit punch	208 mL

a. Jen drinks the apple juice and the water. How many milliliters does she drink in all?

Jen drinks \_\_\_\_\_ mL.

b. Kevin drinks the milk and the fruit punch. How many milliliters does he drink in all?

3. There are 75 students in Grade 3. There are 44 more students in Grade 4 than in Grade 3. How many students are in Grade 4?
4. Mr. Green's sunflower grew 29 centimeters in one week. The next week it grew 5 centimeters more than the previous week. What is the total number of centimeters the sunflower grew in 2 weeks?
5. Kylie records the weights of 3 objects as shown below. Which 2 objects can she put on a pan balance to equal the weight of a 460 gram bag? Show how you know.

<b>Paperback Book</b>	<b>Banana</b>	<b>Bar of Soap</b>
343 grams	108 grams	117 grams